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School code

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School name

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Family name

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Attach your  
barcode ID label here

Book

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of

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books used

External assessment 2022

Question and response book

# Specialist Mathematics

## Paper 1 — Technology-free

### Time allowed

- Perusal time — 5 minutes
- Working time — 90 minutes

### General instructions

- Answer all questions in this question and response book.
- Calculators are **not** permitted.
- QCAA formula book provided.
- Planning paper will not be marked.

### Section 1 (10 marks)

- 10 multiple choice questions

### Section 2 (50 marks)

- 9 short response questions



# Section 1

## Instructions

- Choose the best answer for Questions 1–10.
- This section has 10 questions and is worth 10 marks.
- Use a 2B pencil to fill in the A, B, C or D answer bubble completely.
- If you change your mind or make a mistake, use an eraser to remove your response and fill in the new answer bubble completely.

	A	B	C	D
Example:	<input checked="" type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>

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	A	B	C	D
1.	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>
2.	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>
3.	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>
4.	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>
5.	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>
6.	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>
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8.	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>
9.	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>
10.	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>

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## Section 2

### Instructions

- Write using black or blue pen.
  - Questions worth more than one mark require mathematical reasoning and/or working to be shown to support answers.
  - If you need more space for a response, use the additional pages at the back of this book.
    - On the additional pages, write the question number you are responding to.
    - Cancel any incorrect response by ruling a single diagonal line through your work.
    - Write the page number of your alternative/additional response, i.e. See page ...
    - If you do not do this, your original response will be marked.
  - This section has nine questions and is worth 50 marks.
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**DO NOT WRITE ON THIS PAGE**

**THIS PAGE WILL NOT BE MARKED**

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Do not write outside this box.



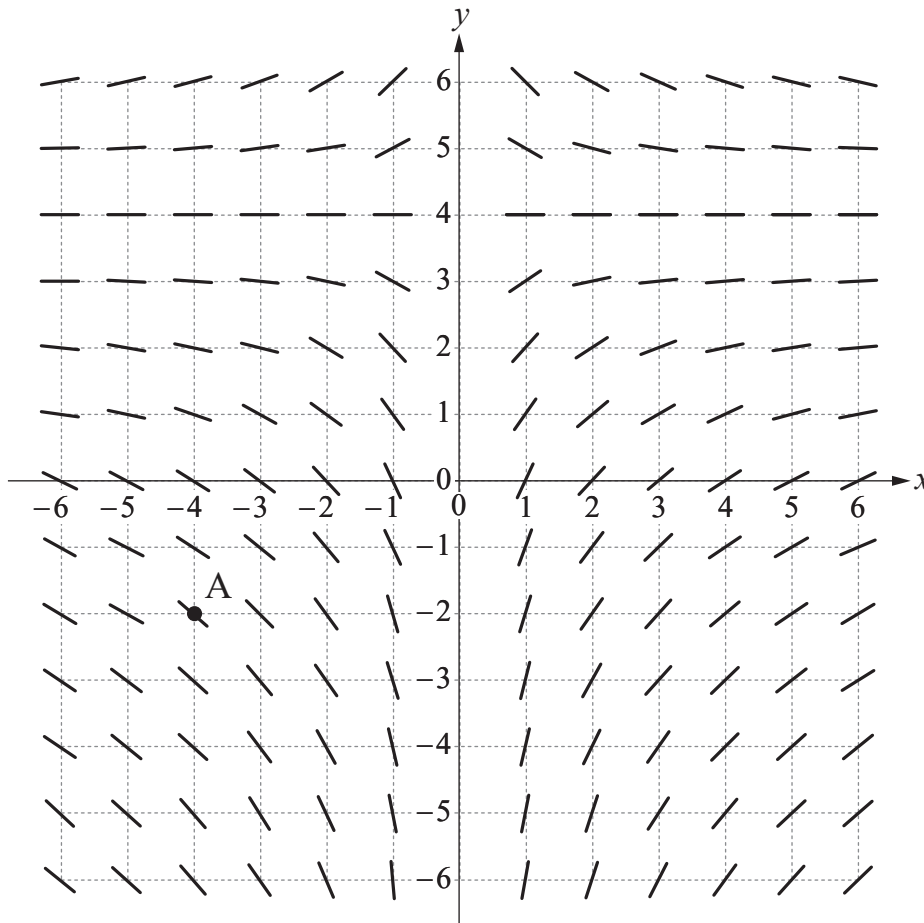






**QUESTION 14 (4 marks)**

The slope field for the differential equation  $\frac{dy}{dx} = \frac{-0.5(y-4)}{x}$ ,  $x \neq 0$  using  $-6 \leq x \leq 6$  and  $-6 \leq y \leq 6$  is shown.



a) Determine the value of the slope at point A.

[2 marks]

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b) Use the slope field to sketch the solution curve for  $\frac{dy}{dx} = \frac{-0.5(y-4)}{x}$  given that when  $x = -6$ ,  $y = 3.5$

[2 marks]

**Note:** If you make a mistake in the slope field, cancel it by ruling a single diagonal line through your work and use the additional response space on page 21 of this question and response book.

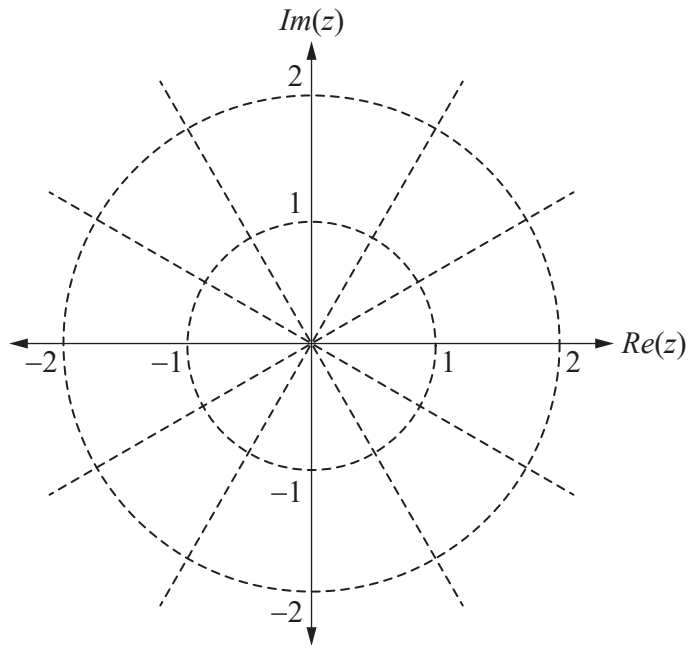
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**QUESTION 15 (4 marks)**

Consider the equation  $z^3 = 1$  where  $z \in \mathbb{C}$ .

- a) Sketch the solutions to  $z^3 = 1$  on the Argand diagram.

[2 marks]



**Note:** If you make a mistake in the Argand diagram, cancel it by ruling a single diagonal line through your work and use the additional response space on page 22 of this question and response book.

The solutions to  $z^3 = 1$  can be expressed in the form  $z = a + bi$ , where  $a, b \in \mathbb{R}$ .

- b) Determine the largest possible positive value of  $ab$ .

[2 marks]

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- b) Use the result from Question 16a) to determine the infinitely many solutions.  
Express your answer in the form of a vector equation of a line.

*[3 marks]*

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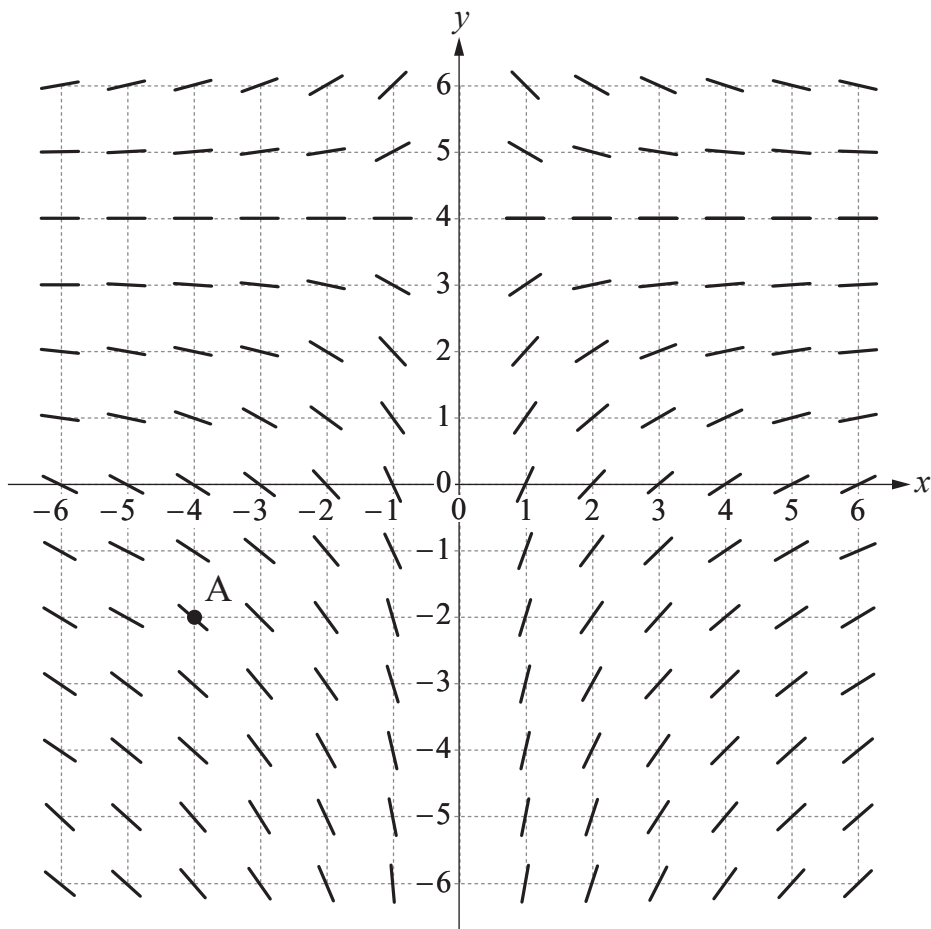






### ADDITIONAL RESPONSE SPACE FOR QUESTION 14b)

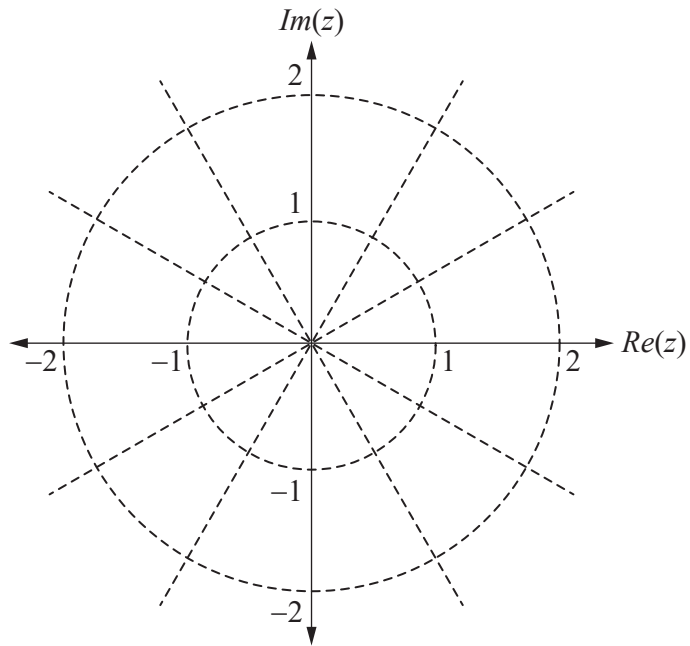
If you want this slope field to be marked, rule a single diagonal line through the slope field on page 9.



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**ADDITIONAL RESPONSE SPACE FOR QUESTION 15a)**

If you want this Argand diagram to be marked, rule a single diagonal line through the Argand diagram on page 10.



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