## Mathematical Methods

## Paper 2 - Technology-active

## General instruction

- Work in this book will not be marked.


## Section 1

## QUESTION 1

The position (in cm ) of a particle is given by $x=\cos (4 t)$, where $t$ is time (in seconds).
The velocity of the particle when $t=5$ is
(A) $1.6323 \mathrm{~cm} \mathrm{~s}^{-1}$
(B) $0.4081 \mathrm{~cm} \mathrm{~s}^{-1}$
(C) $-0.9129 \mathrm{~cm} \mathrm{~s}^{-1}$
(D) $-3.6518 \mathrm{~cm} \mathrm{~s}^{-1}$

## QUESTION 2

Identify the correct features of the function $f(x)=x e^{x}$
(A) $f^{\prime}(-1)=0, f^{\prime \prime}(-1)<0$
(B) $f^{\prime}(-1)=0, f^{\prime \prime}(-1)>0$
(C) $f^{\prime}(-1)<0, f^{\prime \prime}(-1)<0$
(D) $f^{\prime}(-1)<0, f^{\prime \prime}(-1)>0$

## QUESTION 3

The derivative of the function $f(x)$ is given by $f^{\prime}(x)=\sin \left(x^{3}\right)$ for the domain $-1.8<x<1.8$. The number of points of inflection that the graph of $f(x)$ has on this interval is
(A) 1
(B) 3
(C) 4
(D) 5

## QUESTION 4

The distribution for a sample proportion $\hat{p}$ has a mean of 0.15 and a standard deviation of 0.0345 . The sample size is
(A) 10
(B) 14
(C) 107
(D) 116

## QUESTION 5

The continuous random variable $X$ has the probability density function

$$
f(x)=\left\{\begin{array}{cc}
\frac{\cos (x)}{2}, & \frac{-\pi}{2} \leq x \leq \frac{\pi}{2} \\
0, & \text { otherwise }
\end{array}\right.
$$

The standard deviation of $X$ is
(A) 0.467
(B) 0.684
(C) 1.211
(D) 1.467

## QUESTION 6

A stall at the school fete sells cups of lemonade. Assuming the amount of lemonade in a cup is normally distributed with a mean of 60 mL and a standard deviation of $3 \mathrm{~mL}, 80 \%$ of the cups contain more than
(A) 52.4 mL
(B) 57.5 mL
(C) 61.6 mL
(D) 62.5 mL

## QUESTION 7

A marble moves in one direction in a straight line with velocity $v=2 \ln (t+1)$ (in metres per second) where $t$ is time (in seconds) since the marble passed through the origin.
Determine the distance from the origin the marble has rolled after 4 seconds.
(A) 0.40 m
(B) 1.60 m
(C) 3.22 m
(D) 8.09 m

## QUESTION 8

Determine the equation of the asymptote of the function $f(x)=\log _{9}(x-3)-4$.
(A) $x=-4$
(B) $x=-3$
(C) $x=3$
(D) $x=4$

## QUESTION 9

Determine the length of side AB in triangle ABC .

(A) 22.13
(B) 14.44
(C) 9.97
(D) 7.82

## QUESTION 10

The solution of $e^{2 x-3}=42$ is
(A) 1.48
(B) 2.31
(C) 3.37
(D) 4.54

Licence: https://creativecommons.org/licenses/by/4.0 | Copyright notice: www.qcaa.qld.edu.au/copyright — lists the full terms and conditions, which specify certain exceptions to the licence. Attribution: © State of Queensland (QCAA) 2022

