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School code

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School name

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Given name/s

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Family name

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Attach your  
barcode ID label here

Book

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of

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books used

External assessment 2022

Question and response book

# Mathematical Methods

## Paper 1 — Technology-free

### Time allowed

- Perusal time — 5 minutes
- Working time — 90 minutes

### General instructions

- Answer all questions in this question and response book.
- Calculators are **not** permitted.
- QCAA formula book provided.
- Planning paper will not be marked.

### Section 1 (10 marks)

- 10 multiple choice questions

### Section 2 (45 marks)

- 9 short response questions





**DO NOT WRITE ON THIS PAGE**  
**THIS PAGE WILL NOT BE MARKED**



## Section 1

### Instructions

- Choose the best answer for Questions 1–10.
- This section has 10 questions and is worth 10 marks.
- Use a 2B pencil to fill in the A, B, C or D answer bubble completely.
- If you change your mind or make a mistake, use an eraser to remove your response and fill in the new answer bubble completely.

	A	B	C	D
Example:	<input checked="" type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>

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	A	B	C	D
1.	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>
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10.	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>

Do not write outside this box.

## Section 2

### Instructions

- Write using black or blue pen.
  - Questions worth more than one mark require mathematical reasoning and/or working to be shown to support answers.
  - If you need more space for a response, use the additional pages at the back of this book.
    - On the additional pages, write the question number you are responding to.
    - Cancel any incorrect response by ruling a single diagonal line through your work.
    - Write the page number of your alternative/additional response, i.e. See page ...
    - If you do not do this, your original response will be marked.
  - This section has nine questions and is worth 45 marks.
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### QUESTION 11 (5 marks)

Solve for  $x$  in the following.

a)  $\ln(2x) = 5$

[2 marks]

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b)  $\log_4(4x + 16) - \log_4(x^2 - 2) = 1$

[3 marks]

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**QUESTION 12 (3 marks)**

The probability that a debating team wins a debate can be modelled as a Bernoulli distribution. Given that the probability of winning a debate is  $\frac{4}{5}$

- a) Determine the mean of this distribution. *[1 mark]*

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- b) Determine the variance of this distribution. *[1 mark]*

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- c) Determine the standard deviation of this distribution. *[1 mark]*

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**QUESTION 13 (9 marks)**

a) Determine the derivative of  $f(x) = 3e^{2x+1}$

[1 mark]

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b) Given that  $g(x) = \frac{\ln(x)}{x}$ , determine the simplest value of  $g'(e)$ .

[3 marks]

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**QUESTION 14 (6 marks)**

The rate that water fills an empty vessel is given by  $\frac{dV}{dt} = 0.25e^{0.25t}$  (in litres per hour),  $0 \leq t \leq 8\ln(6)$ , where  $t$  is time (in hours).

- a) Determine the function that represents the volume of water in the vessel (in litres). *[2 marks]*

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The vessel is full when  $t = 8\ln(6)$ .

- b) Determine the volume of water, to the nearest litre, the vessel can hold when full. *[2 marks]*

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The table shows the approximate rate the water flows into the vessel at certain times.

$t$	$\frac{dV}{dt}$
0	0.25
1	0.32
2	0.41
3	0.53

- c) Use information from the table and the trapezoidal rule to determine the approximate volume of water in the vessel after three hours.

[2 marks]

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**QUESTION 15 (4 marks)**

The derivative of a function is given by  $f'(x) = e^x(x-4)$ .

Determine the interval on which the graph of  $f(x)$  is both decreasing and concave up.

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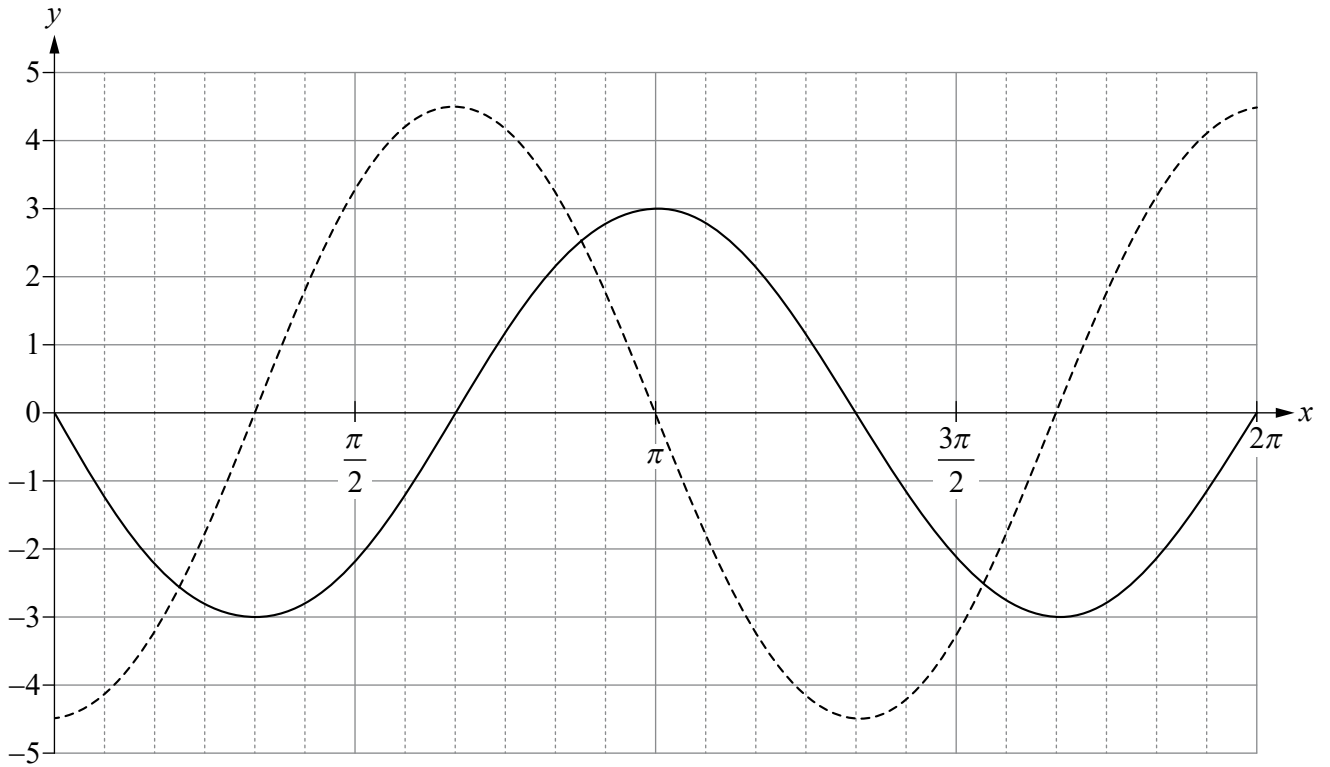
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**QUESTION 16 (3 marks)**

A section of the graphs of the first and second derivatives of a function are shown.

Sketch a possible graph of the function on the same axes over the domain  $0 \leq x \leq 2\pi$ . Explain all reasoning used to produce the sketch.



**Note:** If you make a mistake in the graph, cancel it by ruling a single diagonal line through your work and use the additional response space on page 17 of this question and response book.

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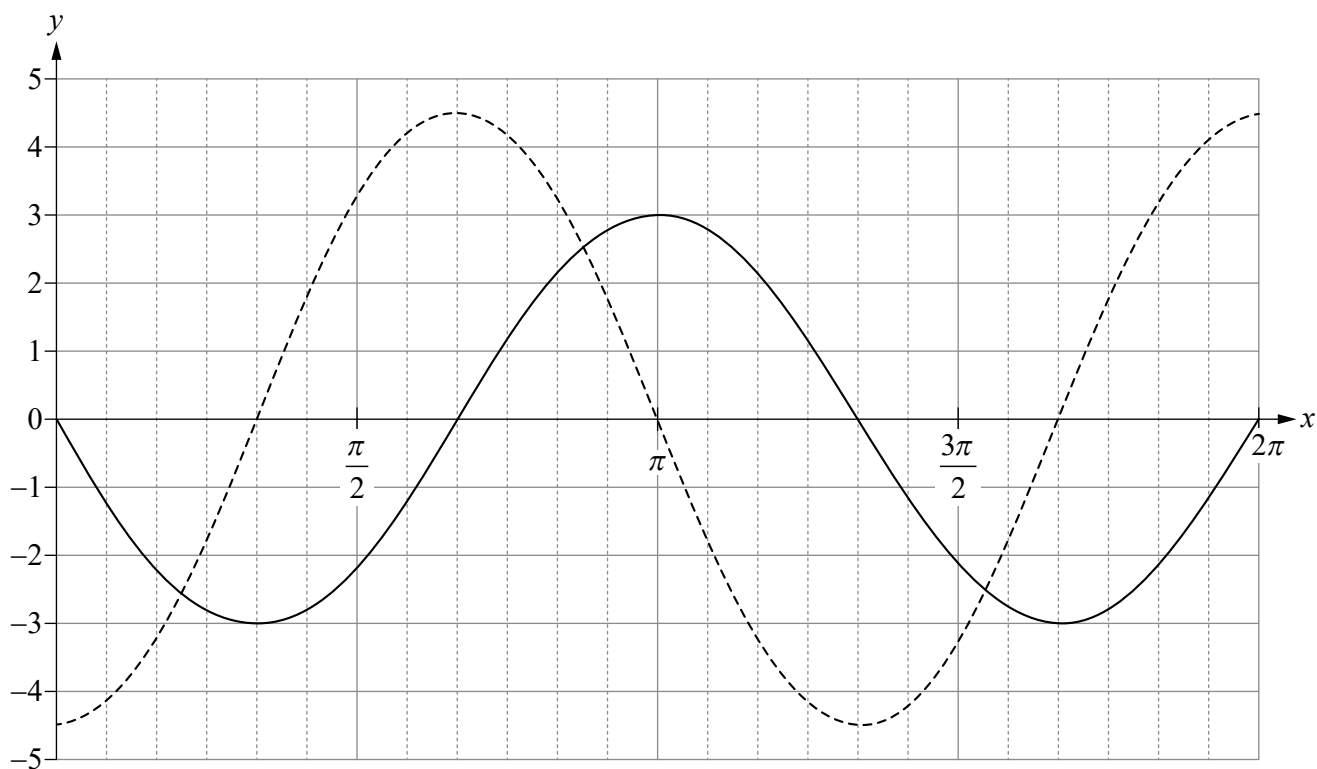






### ADDITIONAL RESPONSE SPACE FOR QUESTION 16

If you want this graph to be marked, rule a single diagonal line through the graph on page 9.



Do not write outside this box.



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