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LUI

Venue code

School name

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Sample assessment 2020

Question and response book

Mathematical Methods

Paper 1 — Technology-free

Time allowed

- Perusal time — 5 minutes
- Working time — 90 minutes

General instructions

- Answer all questions in this question and response book.
- Calculators are not permitted.
- QCAA formula sheet provided.
- Planning paper will not be marked.

Section 1 (10 marks)

- 10 multiple choice questions

Section 2 (50 marks)

- 9 short response questions



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DO NOT WRITE ON THIS PAGE

THIS PAGE WILL NOT BE MARKED

Section 1

Instructions

- Choose the best answer for Questions 1–10.
- This section has 10 questions and is worth 10 marks.
- Use a 2B pencil to fill in the A, B, C or D answer bubble completely.
- If you change your mind or make a mistake, use an eraser to remove your response and fill in the new answer bubble completely.

	A	B	C	D
Example:	<input checked="" type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>

	A	B	C	D
1.	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>
2.	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>
3.	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>
4.	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>
5.	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>
6.	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>
7.	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>
8.	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>
9.	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>
10.	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>

Section 2

Instructions

- Write using black or blue pen.
 - Questions worth more than one mark require mathematical reasoning and/or working to be shown to support answers.
 - If you need more space for a response, use the additional pages at the back of this book.
 - On the additional pages, write the question number you are responding to.
 - Cancel any incorrect response by ruling a single diagonal line through your work.
 - Write the page number of your alternative/additional response, i.e. See page ...
 - If you do not do this, your original response will be marked.
 - This section has nine questions and is worth 50 marks.
-

QUESTION 11 (5 marks)

Determine:

a) $\frac{d}{dx}(3 \ln(5x))$

[1 mark]

b) $\frac{d}{dx}(x^3 \cos(x^4 + 1))$

(You do not need to simplify.) [3 marks]

c) $\int 3e^{4x} dx$

[1 mark]

QUESTION 12 (3 marks)

Simplify the following:

a) $\log_6 9 + 2\log_6 2$

[1 mark]

b) $\frac{\log_3 16}{\log_3 64}$

[2 marks]

QUESTION 13 (4 marks)

Solve the following:

a) $\log_5(2x + 4) = 2$

[2 marks]

b) $\ln(7 - x) - \ln 10 = \ln(x)$

[2 marks]

QUESTION 14 (5 marks)

Let $v(t) = \frac{1}{\pi} + 3\sin(t)$, $t \geq 0$ represent the velocity of an object moving in a straight line.

At $t = \frac{\pi}{3}$, the position of the object is 4.

a) Determine the acceleration function.

[2 marks]

b) Determine the displacement function.

[3 marks]

QUESTION 15 (9 marks)

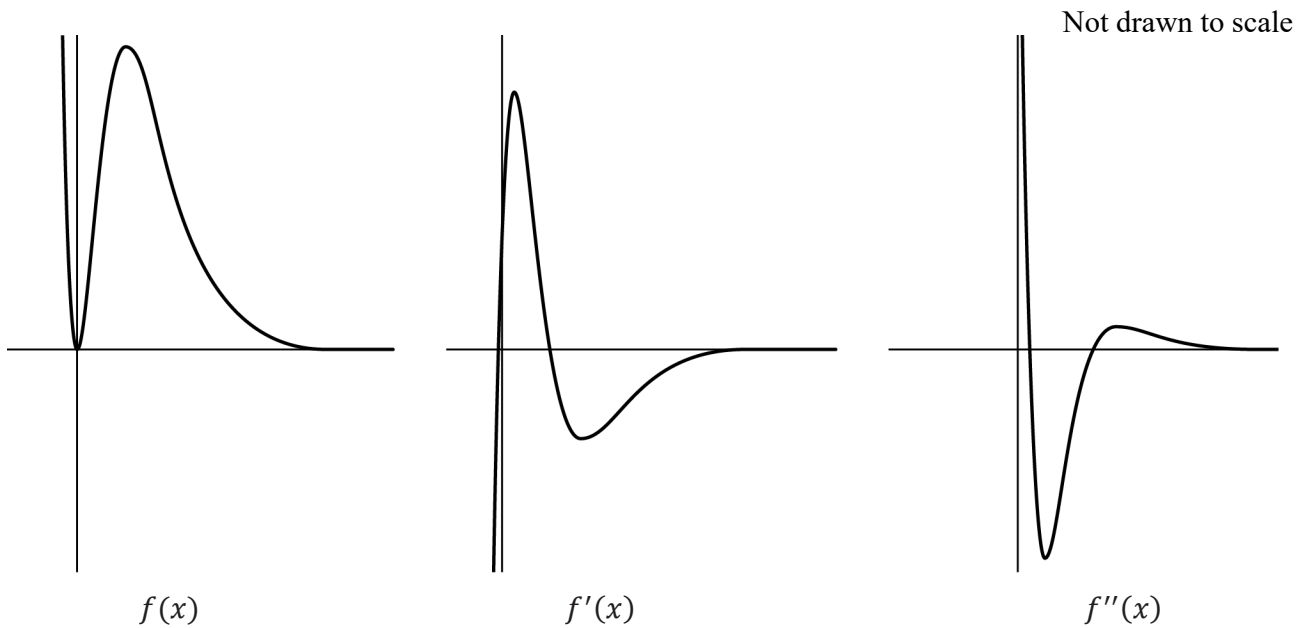
Consider the function: $f(x) = x^2 e^{(-x+4)}$

The first and second derivatives are:

$$f'(x) = x(2 - x)e^{(-x+4)}$$

$$f''(x) = (x^2 - 4x + 2)e^{(-x+4)}$$

The graphs of $f(x)$, $f'(x)$ and $f''(x)$ are shown below:



- a) Determine the coordinates of the local maximum of $f(x)$.

[2 marks]

b) Use the second derivative test to verify the nature of the stationary point from 15a). *[2 marks]*

c) Determine the x -coordinates of any point/s of inflection. *[2 marks]*

d) Determine the intervals where $f(x)$ is concave up and concave down. *[3 marks]*

QUESTION 16 (5 marks)

Determine the equation of the tangent to the function $y = x^3 + ax^2 + bx + 1$ at the point of inflection (1, 6).

QUESTION 17 (7 marks)

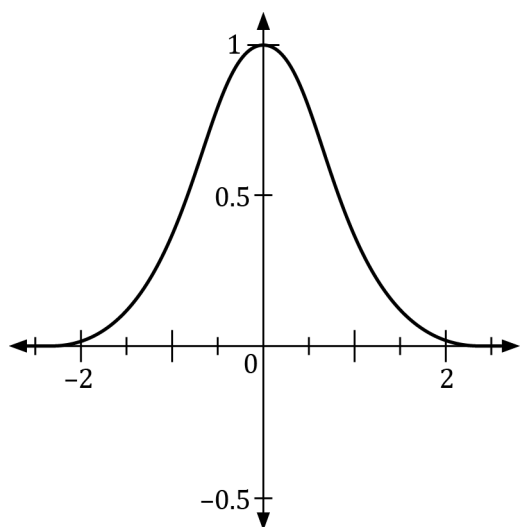
A continuous random variable X has a probability density function f , defined by:

$$f(x) = \begin{cases} a + bx^2 & 0 \leq x \leq 1 \\ 0 & \text{otherwise} \end{cases}$$

If $E(X) = \frac{3}{5}$, determine a and b .

QUESTION 18 (6 marks)

Determine the area of the largest rectangle that has one side on the x -axis and two vertices on the curve $y = e^{-x^2}$. Express your answer in simplest form. The curve is sketched below.



Not drawn to scale

QUESTION 19 (6 marks)

Determine the equation of the tangent to the curve $y = x \ln(x)$ that passes through the point $(0, -e)$.

END OF PAPER

ADDITIONAL PAGE FOR STUDENT RESPONSES

Write the question number you are responding to.

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