# Mathematical Methods 

## Paper 2 - Technology-active

## General instruction

- Work in this book will not be marked.


## Section 1

## QUESTION 1

The limit of $\frac{12^{h}-1}{h}$ as $h$ approaches 0 is closest to
(A) 0.0
(B) 1.0
(C) 2.5
(D) 3.0

## QUESTION 2

The pH of a substance is a measure of its acidity and is given by the formula $\mathrm{pH}=-\log _{10}\left[\mathrm{H}^{+}\right]$where $\left[\mathrm{H}^{+}\right]$is the concentration of hydrogen ions in moles per litre. If a solution has a pH equal to 0.2 , the concentration of hydrogen ions in moles per litre is closest to
(A) 0.32
(B) 0.63
(C) 0.70
(D) 1.58

## QUESTION 3

Let $R$ be the region enclosed by the graph of $y=x e^{x}$, the $x$-axis, and the lines $x=-1$ and $x=1$.
The area of $R$ is closest to
(A) 0.74
(B) 1.26
(C) 2.35
(D) 3.09

## QUESTION 4

Consider the function $f(x)=\log _{p}(x+q)$ where $p>1$ and $0<q<1$.
Which of the following could be the graph of $f(x)$ ?
(A)

(B)

(C)

(D)


## QUESTION 5

An object moves in a straight line with a velocity $v$ given by

$$
v(t)=40\left(e^{-t}-e^{-2 t}\right) \mathrm{m} \mathrm{~s}^{-1} \text { where } t \geq 0
$$

The object is at the origin initially. The displacement-time graph in the first 6 seconds is
(A)

(B)

(C)

(D)


## QUESTION 6

Oil is leaking from a tanker at the rate of $r(t)=9000 e^{-0.2 t}$ litres per hour, where $t$ is in hours.
Determine how much oil leaks from the tanker (to the nearest litre) from time $t=0$ to time $t=10$.
(A) 38910 litres
(B) 8756 litres
(C) 7782 litres
(D) 1556 litres

## QUESTION 7

The records of a shoe manufacturer show that $10 \%$ of shoes made are defective.
Assuming independence, the probability of getting 2 defective shoes in a batch of 20 is
(A) 0.1937
(B) 0.2852
(C) 0.3917
(D) 0.6083

## QUESTION 8

Determine the size of angle $A$ in the triangle.


Not drawn to scale
(A) $48.5^{\circ}$
(B) $61.4^{\circ}$
(C) $118.6^{\circ}$
(D) $131.5^{\circ}$

## QUESTION 9

The displacement of a particle (in metres) at time $t$ (in seconds) is represented by the function

$$
s(t)=t \ln (t)-t, 0<t<4
$$

Determine the approximate acceleration of the particle at time $t=3$.
(A) $0.66 \mathrm{~m} \mathrm{~s}^{-2}$
(B) $0.33 \mathrm{~m} \mathrm{~s}^{-2}$
(C) $-0.33 \mathrm{~m} \mathrm{~s}^{-2}$
(D) $-0.66 \mathrm{~m} \mathrm{~s}^{-2}$

## QUESTION 10

The approximate value of $x$ where the graph of the function $y=x^{3}+6 x^{2}+7 x-2 \cos (x)$ changes concavity is
(A) -3.26
(B) -2.85
(C) -2.20
(D) -1.89

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