## External assessment 2022

# Question and response book 

## General Mathematics

## Paper 1

## Time allowed

- Perusal time - 5 minutes
- Working time - 90 minutes


## General instructions

- Answer all questions in this question and response book.
- QCAA-approved scientific calculator permitted.
- QCAA formula book provided.
- Planning paper will not be marked.


## Section 1 (15 marks)

- 15 multiple choice questions


## Section 2 (42 marks)

- 10 short response questions


## LUI <br> 

## School code



School name

Given name/s
$\square$

## Family name



> Attach your barcode ID label here

## Section 1

## Instructions

- Choose the best answer for Questions 1-15.
- This section has 15 questions and is worth 15 marks.
- Use a 2 B pencil to fill in the $\mathrm{A}, \mathrm{B}, \mathrm{C}$ or D answer bubble completely.
- If you change your mind or make a mistake, use an eraser to remove your response and fill in the new answer bubble completely.

|  | A | B | C | D |
| :---: | :---: | :---: | :---: | :---: |
| Example: |  |  |  |  |
|  |  | $O$ |  |  |



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## Section 2

## Instructions

- Write using black or blue pen.
- Questions worth more than one mark require mathematical reasoning and/or working to be shown to support answers.
- If you need more space for a response, use the additional pages at the back of this book.
- On the additional pages, write the question number you are responding to.
- Cancel any incorrect response by ruling a single diagonal line through your work.
- Write the page number of your alternative/additional response, i.e. See page ...
- If you do not do this, your original response will be marked.
- This section has 10 questions and is worth 42 marks.


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## Question 16 (3 marks)

The table shows the number of sales for a small business in their first six months of trading.

| Time in <br> months, $\boldsymbol{t}$ | Number <br> of sales, $\boldsymbol{n}$ |
| :--- | :--- |
| 1 | 86 |
| 2 | 180 |
| 3 | 160 |
| 4 | 226 |
| 5 | 240 |
| 6 | 335 |

a) Use your calculator to determine the equation of the least-squares line. [1 mark]
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Do not write outside this box.
b) Use the equation from Question 16a) to predict the number of sales in the 21st month. [2 marks]
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## Question 17 (4 marks)

An investment of $\$ 50000$ that compounds interest monthly is modelled by the recurrence relation
$A_{n+1}=1.00375 A_{n}$ where $\mathrm{A}_{0}=50000$.
a) What would be the advertised interest rate per annum, compounding monthly? [2 marks]
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b) How many months would it take for the value of the investment to exceed $\$ 51$ 000? [2 marks]
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## Question 18 (4 marks)

The number of songs on a person's playlist, $n$, in each week since joining a music streaming service, $t$, forms an arithmetic sequence, as shown by the graph.


Use the arithmetic sequence to predict the number of songs on this person's playlist 25 weeks after joining the streaming service.

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Question 19 (4 marks)
The graph shows the amount of rainfall (in mm ) for each quarter from 2016 to 2021.


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a) Describe the long-term trend and seasonality of the time series data.
[2 marks]

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| b) A least-squares line was fitted to the data, with $y$ representing the amount of |
| :--- |
| rainfall and $x$ representing the number of quarters since the beginning of 2016 |
| (e.g. $x=5$ for the first quarter of 2017). |
| $\qquad y=1.763 x+156.5$ |
| Interpret the $y$-intercept and slope of the fitted line. [2 marks] |

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## Question 20 (4 marks)

The table summarises the distances in kilometres (km) between three flower stores and three delivery locations:
$A, B$ and $C$.
Use the Hungarian algorithm to determine the minimum total distance needed to deliver flowers to all locations if each store delivers flowers to only one location.

|  | A | B | C |
| :--- | :--- | :--- | :--- |
| Store 1 | 19 | 17 | 24 |
| Store 2 | 15 | 14 | 22 |
| Store 3 | 23 | 16 | 40 |

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## Question 21 (5 marks)

The paths connecting various landmarks in a park are shown.


## Key

B Bus stop
C Coffee shop
D Duck pond
P Playground
R Rose garden
W Water feature
a) Identify one cycle that passes through the rose garden and the playground. [1 mark]
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b) Identify whether the graph is Eulerian or semi-Eulerian. Justify your response. [2 marks]
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c) Construct an adjacency matrix from the graph, using the vertex order listed in the key. [2 marks]
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## Question 22 (4 marks)

Marovoay and lakora are located on the same meridian at $46.6^{\circ} \mathrm{E}$, as shown on the map of Madagascar.


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a) Determine the latitudes of Marovoay and lakora. [1 mark]
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b) Use the result from Question 22a) to determine the shortest distance between Marovoay and lakora. [3 marks]
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## Question 23 (4 marks)

The least-squares line has been provided for a scatterplot that shows the association between an employee's years of experience, $n$, and their hourly pay, $p$.

a) Given that the least-squares line passes directly through the points $(2,20)$ and $(7,40)$, determine its equation. [2 marks]
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b) Use the equation from Question 23a) to predict the hourly pay of an employee with 15 years experience. [2 marks]
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## Question 24 (5 marks)

The maximum temperature and the number of pies sold each day at a bakery are provided in the table.

| Maximum <br> temperature $\left({ }^{\circ} \mathrm{C}\right)$ | 29 | 20 | 31 | 27 | 23 | 25 | 22 | 33 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Number of pies <br> sold | 32 | 39 | 25 | 33 | 37 | 35 | 37 | 30 |

a) Construct a scatterplot to display the data on the grid provided. [3 marks]
(1)

Note: If you make a mistake in the scatterplot, cancel it by ruling a single diagonal line through your work and use the additional response space at the back of this question and response book.
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b) Describe the association between the maximum temperature and the number of pies sold in terms of direction and strength. [2 marks]
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## Question 25 (5 marks)

A couple borrow money to complete home renovations. Their bank has loaned the amount at $2.4 \%$ p.a. compounding monthly with repayments of $\$ 993.14$ each month for 15 years.
a) Determine the amount of money borrowed. [3 marks]
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b) Write a recurrence relation for the amount owing after $n$ months. [2 marks]
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