# General Mathematics 2019 v1.2 

## Unit 1 Topic 1 high-level annotated sample response

July 2020

## Problem-solving and modelling task

This sample has been compiled by the QCAA to assist and support teachers to match evidence in student responses to the characteristics described in the assessment objectives.

## Assessment objectives

This assessment instrument is used to determine student achievement in the following objectives:

1. select, recall and use facts, rules, definitions and procedures drawn from Unit 1 Topic 1
2. comprehend mathematical concepts and techniques drawn from Unit 1 Topic 1
3. communicate using mathematical, statistical and everyday language and conventions
4. evaluate the reasonableness of solutions
5. justify procedures and decisions by explaining mathematical reasoning
6. solve problems by applying mathematical concepts and techniques drawn from Unit 1 Topic 1.

## Task

## Context

In 2020, Tokyo will host the sixteenth Summer Paralympic Games. A significant number of people will travel to the games to support their country's athletes. These people need to understand the financial requirements of such a trip, including fixed and discretionary spending, in order to develop a personal budget based on their income.

## Task

Investigate the financial requirements of a person aiming to travel from Australia to the Tokyo Paralympic Games in 2020 to support the Australian team. Produce a personal budget based on the results of your mathematical research, then refine the model to ensure they can afford to attend. You are to assume that the supporter:

- has a part-time job
- is entitled to government disability support
- will attend at least four different Olympic events.

You must use:

- the approach to problem-solving and mathematical modelling provided
- different data to other students in your class and school.

You will have four weeks to complete the assessment, including three hours of class time.

## Sample response

| Criterion | Marks allocated | Result |
| :--- | :--- | :--- |
| Formulate <br> Assessment objectives 1, 2,5 |  |  |
| Solve <br> Assessment objectives 1, 6 |  |  |
| Evaluate and verify <br> Assessment objectives 4,5 |  |  |
| Communicate <br> Assessment objective 3 |  |  |
| Total |  |  |

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## Communicate

coherent and
concise organisation, appropriate to the genre

## Formulate

accurate translation of all aspects of the problem by identifying mathematical concepts and techniques

## Formulate

accurate
documentation of relevant observations
documentation of appropriate assumptions

## 1 Introduction

The aim of this report is to investigate the financial requirements for a person saving to be a spectator at the next Paralympic Games, which will be held in Tokyo, Japan from 25 August to 6 September 2020 (Disabled World 2017).

To create a personal budget for the person to ensure they can attend the Paralympics, I will investigate suitable government allowances available to them and then create a weekly budget using a spreadsheet program. The budget will be used to save for the trip. The total amount of money required will need to include:

- airfares, including increases due to inflation (using the compound interest formula)
- accommodation
- travel insurance
- spending money for entertainment and extra meals.

Once I have calculated the amount of money in Australian dollars, this amount will need to be converted into Japanese yen. For this calculation, I will observe the conversion rate once a week for the next three weeks and use the mean.

Note: The mathematical concepts I will use to investigate this problem are shown in bold type above.

## 2 Initial Considerations Observations and Assumptions

1. The task states that the supporter is entitled to government disability support and has a part-time job. Looking at the available support online it would seem that the 'Disability Support Pension' is the most appropriate (Department of Human Services 2017a) with a base rate of $\$ 808.30$ each fortnight.
2. The task also states that the supporter has a part-time job. I will assume that the supporter earns the maximum fortnightly amount that will not affect their Disability Support Pension. Therefore, they will earn \$164 (Department of Human Services 2017b) each fortnight from a part-time job.
3. The cost of airfares can vary significantly. Looking at various websites it seems that buying tickets well in advance and for non-direct flights are cheaper. Therefore, the tickets chosen for this investigation will be the cheapest available bought well in advance.
4. Exchange rates change daily, so it is important to look for the best rates. For this investigation I have used an exchange rate of 1 AUD $=86.8739$ JPY found in Appendix 3 at www.xe.com/currencyconverter/convert/?Amount=1\&From=AUD\&To=JPY
5. I have assumed that the person lives in Brisbane, already has a passport and is 21.

|  | 6. Travel insurance needs to be taken out for the trip. I will assume no major injury occurs outside stipulated health insurance conditions on the trip, as this could cause extra unexpected expenses. |
| :---: | :---: |
|  | 7. The person plans to see four different events, which will be held at a variety of venues in Tokyo. The maximum price is expected to be 6000 Yen per ticket, so I will assume that all 4 tickets are the maximum expected price. <br> 8. For budgeting the regular expenses are estimates based on averaging information sourced from family and friends. |
|  | 3 Developing the budget |
|  | 3.1 Income |
| Communicate | 3.1.1 Government allowances |
| correct us vocabulary to develop the response | The government allowance available for this person is a Disability Support Pension (Department of Human Services 2017a). Government payments also available for someone receiving a pension are the pension supplement energy supplement and rent assistance. |
| Formulate accurate | \$808.30 pension basic rate |
| relevant | + $\$ 65.90$ pension supplement |
|  | + \$14.10 energy supplement |
| Communicate coherent and | + \$130.60 rent assistance |
| concise <br> organisation of | = \$1018.90/fortnight |
| the response. |  |
| which can be <br> read | Total government allowances per fortnight: \$1018.90 |
| independently of the task | 3.1.2 Part-time iob |
| Formulate accurate documentation of relevant observations | The person can earn up to $\$ 164$ per fortnight without affecting their pension. If they earn more than this amount, their pension will be reduced by 50 cents for each dollar over $\$ 164$ (Department of Human Services 2017b). |
| documentation of appropriate assumptions | The person will work part-time at their local corner shop at a rate of $\$ 19.44 /$ hour (Fair Work Ombudsman 2017). They want to work the maximum number of hours without affecting their pension. |
| Solve <br> application of | Maximum allowable hours |
| concepts and | \$164 |
| 隹 | $\overline{\$ 19.44 / \mathrm{hr}}=8.4362$ hours/fortnight |
|  | Therefore, they will work eight hours (rounded down to nearest hour) per fortnight, or four hours per week. |
|  | 3.1.3 Total income |

## Communicate

coherent and
concise
organisation of the response. which can be
read
independently of the task

## Formulate

accurate
documentation of relevant observations

## Solve

application of mathematical concepts and techniques
Communicate correct use of appropriate procedural vocabulary to develop the response

Part-time job income: $8 \times \$ 19.44=\$ 155.52 /$ fortnight
Total fortnightly income: $\$ 1018.90+\$ 155.52=\$ 1174.42 /$ fortnight

### 3.2 Expenses

### 3.2.1 Airfares

Flights cannot be booked three years in advance, so I looked at fares for 24 August to 7 September 2017 and applied increases according to inflation to estimate the future costs. I used a flight comparison website and found 383 flight options. The best return price was $\$ 924$ with Thai Airways; however, flights were over 32 hours each way and arrived very late at night. The most expensive return flights were with British Airways at \$9702, and did not leave either country on the correct days. Most flights had at least one stopover.

I decided on a Singapore Airlines return flight because it is about 20 hours each way. The flights stop in Singapore and cost only $\$ 1060.95$ in total.

### 3.2.2 Travel insurance

Travel insurance of $\$ 116.13$ covers overseas emergency assistance, medical and hospital coverage, cancellation and luggage protection.

### 3.2.3 Airfares, travel insurance and Paralympic tickets (see Appendix 1)

## Paralympic tickets

Event ticket cost $=6000$ Yen $\times 4$

$$
\begin{aligned}
& =24000 \text { Yen } \\
& =24000 \div 86.8739 \text { AUD } \\
& =\$ 276.26
\end{aligned}
$$

## Total upfront expenses

Airfares + travel insurance + event ticket cost $=\$ 1060.95+\$ 116.13+\$ 276.26$

$$
=\$ 1453.34
$$

## Increase due to inflation

These costs are likely to increase over the next three years due to inflation, so I will calculate the future increased cost. The Australian annual inflation rate fluctuates (Rate Inflation 2017). I calculated the mean of the rate from 2012 to 2016.

$$
\frac{1.3+1.5+2.5+2.5+1.7}{5}=1.9
$$

The average inflation rate was $1.9 \%$ over the past five years.
Using the 2017 airfare, travel insurance and event ticket cost of \$1453.34 and applying an increase in price of $1.9 \%$ due to inflation will find the predicted cost in 2020.


## 4Budget summary

A budget needs to be prepared that includes:

- person's regular income
- person's regular expenses
- savings required for the Paralympics trip.


### 4.1 Regular income

The person's regular income is $\$ 1174.42$ /fortnight from government allowances and their part-time job. See section 3.1.

### 4.2 Regular expenses

The person's regular expenses include food, electricity, health insurance, rent, entertainment and necessities such as clothing and shoes. Estimated values are given in the spreadsheet below based on research online and comparing with family and friends.
accurate and appropriate use of technology; accurate use of complex procedures to reach a valid solution The solution consists of an involved combination of parts that are connected.

## Solve

application of mathematical concepts and techniques relevant to the task


See Appendix 5 for budget spreadsheet calculations.


Communicate
coherent and
concise
organisation of
the response ${ }_{2}$ appropriate to
the genre

## Evaluate and

 verifyjustification of decisions made using mathematical reasoning

## Evaluate and

## verify

evaluation of the reasonableness of solutions by considering the results, assumptions and obsservations

Sell the car and use public transport. Although public transport will be a new cost, it will only be $\$ 9.36 /$ week (see Appendix 2). The savings in the first year are listed below, and greater savings will be made in the following years due to increased costs for these items.

1. No car payments, saving $\$ 120 /$ week.
2. No petrol needed, saving $\$ 40 /$ week.
3. No car servicing, saving $\$ 120$ every 6 months.
4. No car insurance, saving $\$ 310$ every 6 months.

These calculations are included in the budget in Appendix 5.

### 5.3 Excess currency

At the end of the trip there may be some Japanese currency unspent. It is assumed that the amount remaining will be $10 \%$ of the amount originally budgeted for.
$¥ 121623.46 \times 10 \%=¥ 12162.346$
The exchange rate has changed from the start of the trip to when they returned to Australia. See Appendix 4.

### 5.3.1 Converting remaining yen back to Australian dollars

$12162.346 \times 0.011=133.79$
Remaining Japanese yen converted back to Australian dollars would be \$133.79.

### 5.4 Amount required to save for trip

The original budgeted amount required was $\$ 5750$.
With the new budget, outlined below, they will have saved $\$ 7052.71$, prior to the Tokyo games, which is more than they need. Therefore, they can now afford the trip.

## Communicate

 correct use of technical vocabulary and conventions to develop the response, appropriate to the genre
## Communicate

coherent and
concise organisation of the response ${ }_{2}$ including a suitable introduction, body and conclusion, which can be read independently of the task sheet


See Appendix 5 for budget formula spreadsheet.

## 6Conclusion

In the original budget, the spectator could not afford to attend the Paralympics. By making some lifestyle changes they can now afford the trip.

The new budget results in savings of $\$ 7052.71$.
The spectator needs $\$ 5750$ to fund the trip. Therefore they can now afford the trip. The budget takes into consideration likely price increases due to inflation but also includes reduced spending on non-essential items.

### 6.1 Recommendations

Further recommendations regarding the budget would be to include the Consumer Price Index (CPI). Some calculations have included increased costs due to inflation; however, a standard increase due to the CPI would more thoroughly cover predicted costs.

## 7 Appendixes

## Appendix 1

Airfare for 24 August (Brisbane-Singapore-Tokyo)


Airfare for 7 September (Tokyo-Singapore-Brisbane)


Travel insurance and total airfare cost


Information gathered on 20 March 2017 from www.webjet.com.

## Appendix 2

South East Queensland go card fees.

## Concession

| Zones <br> travelled | go card | go card <br> off-peak | Single paper ticket |
| :---: | :---: | :---: | :---: |
| 1 | $\$ 1.60$ | $\$ 1.28$ | $\$ 2.30$ |
| 2 | $\$ 1.95$ | $\$ 1.56$ | $\$ 2.80$ |
| 3 | $\$ 2.98$ | $\$ 2.38$ | $\$ 4.30$ |
| 4 | $\$ 3.93$ | $\$ 3.14$ | $\$ 5.70$ |
| 5 | $\$ 5.16$ | $\$ 4.13$ | $\$ 7.50$ |
| 6 | $\$ 6.55$ | $\$ 5.24$ | $\$ 9.50$ |
| 7 | $\$ 8.14$ | $\$ 6.51$ | $\$ 11.80$ |
| 8 | $\$ 9.66$ | $\$ 7.73$ | $\$ 14.00$ |

## Weekly transport costs:

Off peak, 2 zones, 3 days/week
$(\$ 1.56 \times 2) \times 3=\$ 9.36 /$ week

Information gathered on 20 March 2017 from www.translink.com.au/tickets-and-fares/fares-and-zones/current-fares.

## Appendix 3

## 1 AUD $=86.8739 \mathrm{JPY}$

Australian Dollar $\leftrightarrow$ Japanese Yen<br>1 AUD = 86.8739 JPY $1 \mathrm{JPY}=0.0115109$ AUD

Information gathered on 20 March 2017 from www.xe.com/currencyconverter/convert/?Amount=1\&From=AUD\&To=JPY.

## Appendix 4

## Convert currencies



Last updated 21 March 8:39 AM - Data from Morningstar

Information gathered on 20 March 2017 from
www.bing.com/search?q=japanese+yen+to+australain+dollars\&src=IESearchBox\&FORM=IENTSR.

## Appendix 5

| Unit 1 Budget |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Solve with formulas |  |  |  |  |  |
| Years 2017-2020 | Half year | Whole year | Whole year | Half year |  |
|  | July-Dec 2017 | Jan-Dec 2018 | Jan-Dec2019 | Jan-June 2020 | Total |
| Income |  |  |  |  |  |
| Income - no tax (increasing by 3\%p.a.) | $=((808.3+65.9+14.1+130.6)+155.52) * 26 / 2$ | =B5*2*1.03 | =C5*1.03 | =D5*1.03/2 | =SUM(B5:E5) |
| Expenses |  |  |  |  |  |
| Food (\$130/w, increasing by 5\% annually) | $=130 *(52 / 12) * 6$ | $=130 *(52 / 12) * 12 * 1.05$ | = C8*1.1 | =D8*1.1/2 | =SUM(B8:E8) |
| Electricity (\$580/quarter, up 10\% p.a.) | $=580 * 4 / 2$ | $=580 * 4 * 1.1$ | = C9*1.1 | =D9*1.1/2 | =SUM(B9:E9) |
| Biannual Insurance (\$310, up 10\% pa) | =620/2 | =B10*2*1.1 | =C10*1.1 | =D10*1.1/2 | =SUM(B10:E10) |
| Rent Payments (\$350/week, up by 5\% p.a.) | $=350 * 26$ | =B11*2*1.05 | =C11*1.1 | =D11*1.1/2 | =SUM(B11:E11) |
| Car Loan Payments (\$120/week, constant) | $=120 * 26$ | =B12*2 | =B12*2 | =B12 | =SUM(B12:E12) |
| Clothing/Shoes (\$150/m, up 10\% p.a.) | $=150 * 6$ | =B13*1.1*2 | $=C 13 * 1.1$ | =D13*1.1/2 | =SUM(B13:E13) |
| Entertainment (\$220/w, constant) | $=220 * 26$ | = B14*2 | =C14 | =B14 | =SUM(B14:E14) |
| Medical Expenses (\$80/w, up 15\% p.a.) | =80*26 | =B15*2*1.15 | =C15*1.15 | =D15*1.15/2 | =SUM(B15:E15) |
| Petrol (\$40/week, increasing by 5\% p.a.) | $=40 * 26$ | =B16*2*1.05 | =C16*1.05 | =D16*1.05/2 | =SUM(B16:E16) |
| Car Servicing (\$120, twice a year, constant) | $=120$ | =B17*2 | =B17*2 | =B17 | =SUM(B17:E17) |
| Telephone Bill (\$50/m 2yr plan, \$60/m 2yr) | $=50 * 6$ | = B18*2 | =60*12 | = D18/2 | =SUM(B18:E18) |
| Miscellaneous (\$50/week, constant) | $=50 * 26$ | =B19*2 | =B19*2 | =B19 | =SUM(B19:E19) |
| Total Expenses | =SUM(B8:B19) | =SUM(C8:C19) | =SUM(D8:D19) | =SUM(E8:E19) | =SUM(B21:E21) |
| Bank Balance (Start of Year) | 20 | = ${ }^{\text {2 }}$ 25 | =C25 | =D25 |  |
| Surplus/Deficit | = B5-B21 | =C5-C21 | = D5-D21 | =E5-E21 | =SUM(F5-F21) |
| Bank Balance (End of Year) | = $\mathrm{B} 24+\mathrm{B} 23$ | $=\mathrm{C} 24+\mathrm{C} 23$ | =D24+D23 | =E24+E23 |  |
| Savings | = $\mathrm{B} 23+\mathrm{B} 24$ | = $\mathrm{B} 26+\mathrm{C} 24$ | $=C 26+D 24$ | =D26+E24 | =E26 |
| Percentage of Income | = $\mathrm{B} 24 / \mathrm{B5}$ | =C24/C5 | =D24/D5 | =E24/E5 | =F24/F5 |
|  |  |  |  |  |  |



## Appendix 6

YUMA IN RESIDENTIAL, SETAGAYA
Showing 1 homestay
Let's have a local experience with us. I can offer making ordinary Jopanese eating
meals with you. I will toke you to hot spring with a bicycl.
Distance from centre of Y UMA: 2.2 km
FROM $\$ 63$ PER NIGHT

## 8Reference list

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