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Teacher $\square$ Class $\square$

School name $\square$

## Essential Mathematics

## Time allowed

- Perusal time - 5 minutes
- Working time - 60 minutes


## General instructions

- Answer all questions in this question and response book.
- Write using black or blue pen.
- QCAA-approved calculator permitted.
- Ruler required.
- QCAA formula book provided.
- Planning paper will not be marked.

Part A: Simple (40 marks)

- 9 short response questions

Part B: Complex (10 marks)

- 2 short response questions


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## Instructions

- Questions worth more than one mark require mathematical reasoning and/or working to be shown to support answers.
- If you need more space for a response, use the additional pages at the back of this book.
- On the additional pages, write the question number you are responding to.
- Cancel any incorrect response by ruling a single diagonal line through your work.
- Write the page number of your alternative/additional response, i.e. See page ...
- If you do not do this, your original response will be marked.


## Part A: Simple

- This part has nine questions and is worth 40 marks.


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## QUESTION 1 (3 marks)

A school is constructing a bus stop to accommodate five buses, as shown from the side view.


Not to scale
a) Estimate the minimum length of the bus stop in centimetres.
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$\qquad$
b) Convert the result from Question 1a) to metres.

## QUESTION 2 (5 marks)

A cylindrical rainwater tank is installed at a property, as shown.

a) Calculate the volume of the rainwater tank. [2 marks]
$\qquad$
$\qquad$
$\qquad$
b) Use the result from Question 2a) to determine the capacity of the rainwater tank in kilolitres.
c) Use the result from Question 2b) to calculate the number of tanks needed to collect 250 kL of rainwater.
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## QUESTION 3 (3 marks)

A storage box is in the shape of a cube.
Not to scale

$\longleftarrow 19.8 \mathrm{~cm} \longrightarrow$
a) Round the side length of the storage box to the nearest centimetre.
[1 mark]
b) Use the result from Question 3a) to estimate the area of one face of the storage box in square centimetres.
$\qquad$
$\qquad$
$\qquad$
c) Use the result from Question 3b) to estimate the volume of the storage box in cubic centimetres.

## QUESTION 4 (5 marks)

A person's body oxygen level test (BOLT) score measures the number of seconds a person lasts before feeling the need to take a breath. The five-number summary for individual scores in order is $26,27,30$, 34 and 45.
a) Use the five-number summary to construct a box plot.

Draw your box plot here.


Note: If you make a mistake in the box plot, cancel it by ruling a single diagonal line through your work and use the additional response space at the back of this question and response book.
b) Describe the spread of the box plot for the BOLT scores.
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## QUESTION 5 (5 marks)

A glass pyramid is filled with coloured liquid as a prop for a play.

a) Calculate the volume of the pyramid in cubic metres.
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$\qquad$
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$\qquad$
b) Use the result from Question 5a) to calculate the capacity of the pyramid in litres.
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$\qquad$

It is known that 1 L of coloured liquid has an estimated mass of 0.9 kg .
c) Use the result from Question 5 b) to estimate the mass, in kilograms, of coloured liquid needed to fill the pyramid.

## QUESTION 6 (4 marks)

A coach recorded the heights of a Year 5 class in centimetres and displayed the results in the table.

| 125 | 98 | 102 | 100 | 120 | 103 | 118 | 110 | 120 | 125 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

Complete the five-number summary for the heights by writing an appropriate label or value in each empty cell of the table.

| Minimum |  | Median | Upper quartile $\left(\mathrm{Q}_{3}\right)$ |  |
| :---: | :---: | :---: | :---: | :--- |
|  | 102 |  | 120 |  |

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## QUESTION 7 (5 marks)

A school built the rectangular volleyball court shown.
$\square$
Scale 1:200
a) Calculate the actual length and width of the volleyball court in centimetres.

Length: $\qquad$
$\qquad$

Width: $\qquad$
$\qquad$
b) Use the results from Question 7a) to calculate the perimeter of the volleyball court in metres.
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## QUESTION 8 (4 marks)

A survey revealed the annual amount of money students saved in dollars.

| 500 | 500 | 750 | 750 | 1000 | 1250 | 1250 | 1500 | 1500 | 1750 | 1750 | 1750 | 2250 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

a) Determine the modal amount of money saved.
$\qquad$
$\qquad$
b) Calculate the mean amount of money saved.
$\qquad$
$\qquad$
$\qquad$
$\qquad$

The company running the survey claims that the mean amount of money saved is greater than the modal amount of money saved.
c) Use the results from Questions 8a) and 8b) to evaluate the reasonableness of their claim. [1 mark]
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## QUESTION 9 (6 marks)

A farmer is planting crops in the paddock shown.

Not to scale

a) Identify the name of the two-dimensional shape.
[1 mark]
b) How many vertices does the paddock have?
[1 mark]
$\qquad$
$\qquad$
c) Calculate the area of the paddock in square metres.
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d) Convert the result from Question 9c) to hectares.
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## Part B: Complex

- This part has two questions and is worth 10 marks.


## QUESTION 10 (5 marks)

A student created a cardboard model of a square-based pyramid as shown.

a) Use trigonometry to calculate the slant height, $h$, of the triangular face in centimetres.
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b) Use the result from Question 10a) to calculate the total surface area of the model in square centimetres.
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## QUESTION 11 (5 marks)

A teacher claims that, on average, students in their Year 12 class are taller than students in their Year 11 class.
The data for the student heights is displayed in the back-to-back stem-and-leaf plot.

| Leaf: Year 12 class | Stem | Leaf: Year 11 class |
| ---: | ---: | :--- |
|  | 16 | 79 |
| 965332210 | 17 | 013368 |
| 71 | 18 | 11 |
|  | 19 | 7 |

Key: $17 \mid 6=176 \mathrm{~cm}$

Investigate the suitability of using measures of central tendencies, excluding the mode, to evaluate the reasonableness of the teacher's claim. Justify your decision using mathematical reasoning.

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## ADDITIONAL PAGE FOR STUDENT RESPONSES

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## ADDITIONAL PAGE FOR STUDENT RESPONSES

If you want this box plot to be marked, rule a single diagonal line through your original response.

Draw your box plot here.



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